

6.2 - Inverse Relations and Functions · Form A

All work must be completed on a separate sheet of paper, in a clear and organized manner. Final answers only on WS.

Example 1

For each polygon, find the inverse of the relation. Then, graph both the original relation and its inverse.

1. $\triangle XYZ$ with vertices at $\{(7, 7), (4, 9), (3, -7)\}$ $\{(7, 7), (9, 4), (-7, 3)\}$

2. quadrilateral $FGHJ$ with vertices at $\{(4, 3), (-4, -4), (-3, -5), (5, 2)\}$ $\{(3, 4), (-4, -4), (-5, -3), (2, 5)\}$

Examples 2 and 3

Find the inverse of each function. Then graph the function and its inverse. If necessary, restrict the domain of the inverse so that it is a function.

3. $g(x) = 5x$ $g'(x) = \frac{1}{5}x$

4. $h(x) = \frac{x-4}{3}$ $h'(x) = 3x+4$

5. $g(x) = x+4$ $g'(x) = x-4$

6. $f(x) = -8x+9$ $f'(x) = -\frac{1}{8}x + \frac{9}{8}$

7. $h(x) = x^2 + 4$ $h'(x) = \pm\sqrt{x-4}$

Example 4

8. **CRYPTOGRAPHY** DeAndre is designing a code to send secret messages. He assigns each letter of the alphabet to a number, where A = 1, B = 2, C = 3, and so on. Then he uses $c(x) = 4x - 9$ to create the secret code.

a. Find the inverse of $c(x)$, and describe its meaning. $c^{-1}(x) = \frac{1}{4}x + \frac{9}{4}$

b. Make tables of $c(x)$ and $c^{-1}(x)$. Use the table to decipher the message: 15, 75, 47, 3, 71, 27, 51, 47, 67. **Functions**

Examples 5

Determine whether each pair of functions are inverse functions. Write yes or no.

9. $f(x) = 2x + 3$
 $g(x) = \frac{1}{2}(x-3)$ **yes**

10. $f(x) = 2x$
 $g(x) = \frac{1}{2}x$ **yes**

11. $f(x) = 8x - 10$
 $g(x) = \frac{1}{8}x + \frac{5}{4}$ **yes**

Examples 6

12. **GEOMETRY** The formula for the area of a trapezoid is $A = \frac{h}{2}(a+b)$. Determine whether $h = 2A - (a+b)$ is the inverse of the original function. **no**

Mixed Exercises

Find the inverse of each function. Then graph the function and its inverse. If necessary, restrict the domain of the inverse so that it is a function.

13. $f(x) = 3x$ $f^{-1}(x) = \frac{1}{3}x$

14. $g(x) = 2x - 1$ $g'(x) = \frac{1}{2}x + \frac{1}{2}$

15. $f(x) = (x+1)^2 + 3$
 $f^{-1}(x) = \pm\sqrt{x-3} - 1$

Determine whether each pair of functions are inverse functions. Write yes or no.

16. $f(x) = \frac{1}{3}x^2 + 1$ *yes*
 $g(x) = \sqrt{3x - 3}$

17. $f(x) = \frac{2}{3}x^3$ *no*
 $g(x) = \sqrt{\frac{2}{3}x}$

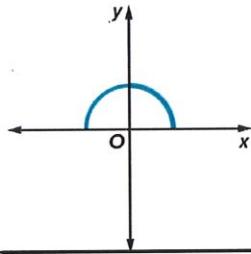
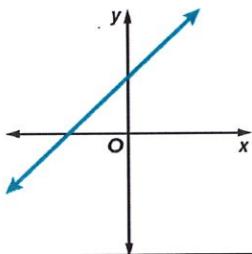
18. $f(x) = 2\sqrt{x - 5}$ *no*
 $g(x) = \frac{1}{4}x^2 - 5$

Restrict the domain of $f(x)$ so that its inverse is also a function. State the restricted domain of $f(x)$ and the domain of $f^{-1}(x)$.

19. $f(x) = 3x^2$ *no* 20. $f(x) = \sqrt{x + 3}$

Sketch a graph of the inverse of each function. Then state whether the inverse is a function.

21. *Graph of a linear function passing through the origin with a positive slope.*



23. Graph the inverse of the piecewise function shown.

24. Use the table to find the relationship between $(f+g)^{-1}(x)$ and $f^{-1}(x) + g^{-1}(x)$.

a. Suppose that functions $f(x)$, $g(x)$, and $(f+g)(x)$ all have inverse functions defined on the domain $[0, 3]$. Calculate the following values.

i. $f^{-1}(3) + g^{-1}(3) =$

ii. $f^{-1}(1) + g^{-1}(1) =$

b. Use the value of $(f+g)(1)$ to find $(f+g)^{-1}(3)$. Use the value of $(f+g)(0)$ to find $(f+g)^{-1}(1)$.

c. Joyce claims that $(f+g)^{-1}(x) = f^{-1}(x) + g^{-1}(x)$. Determine whether she is correct. Explain your reasoning.

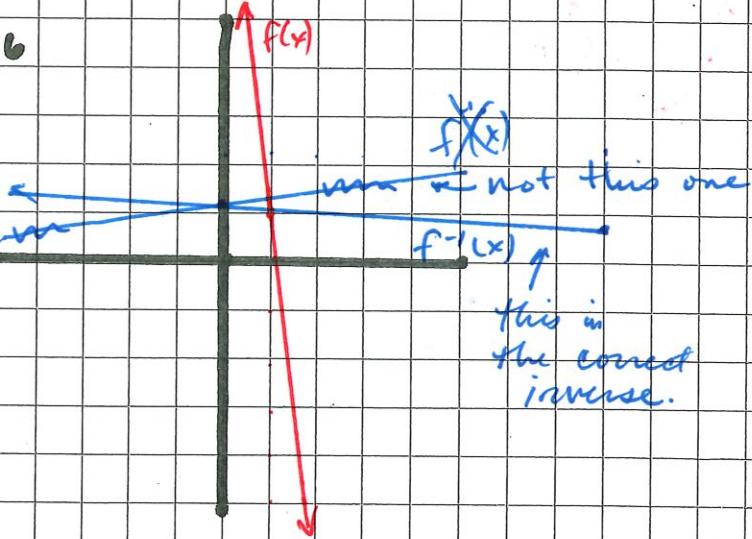
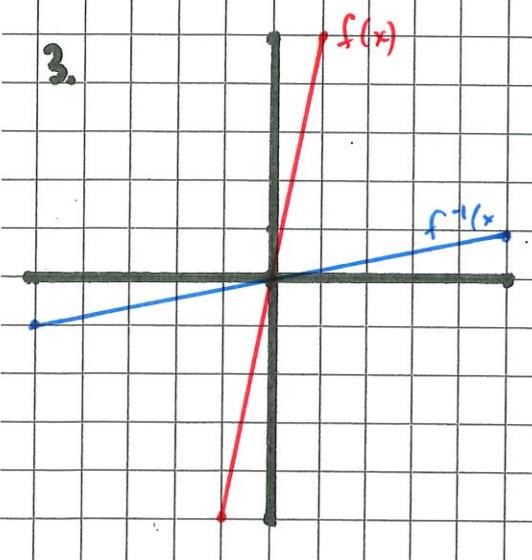
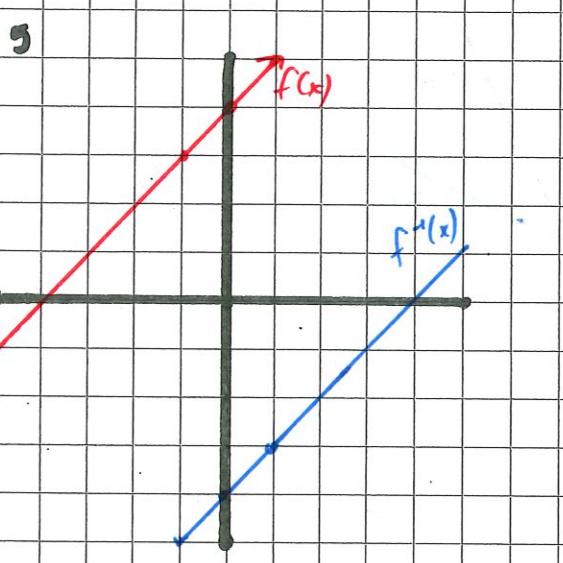
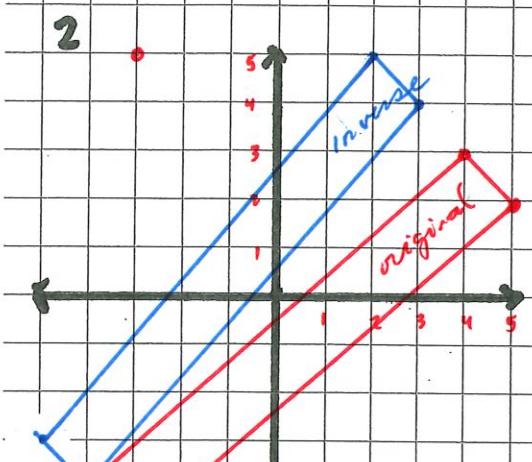
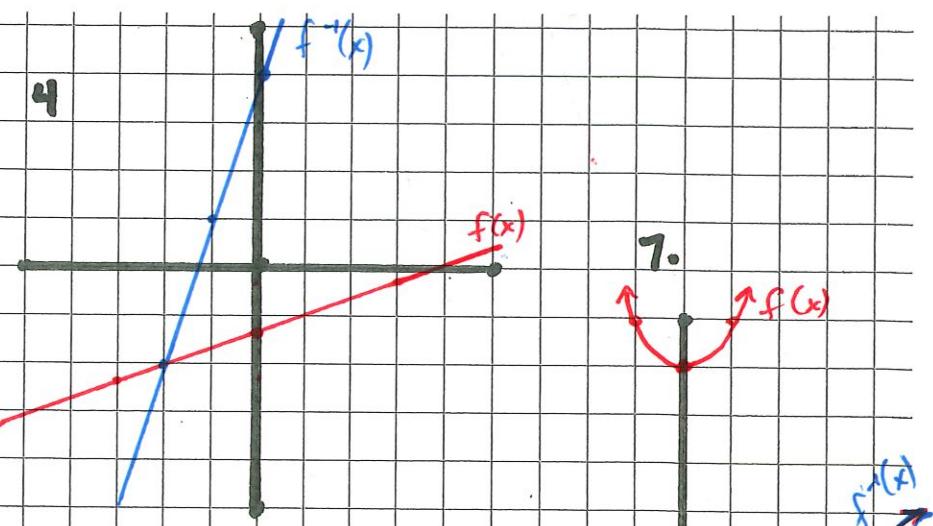
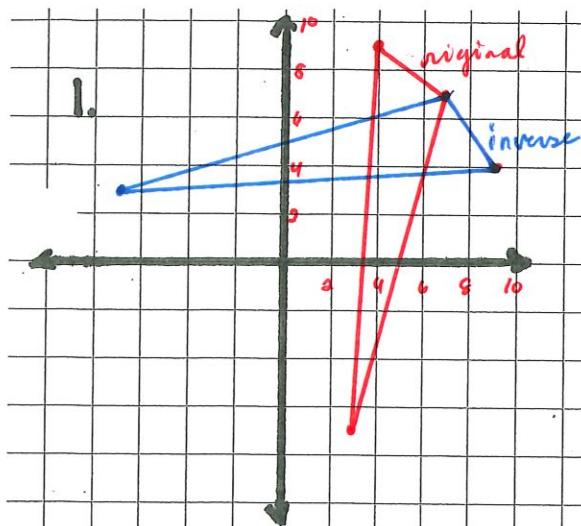
d. Consider the functions $f(x) = 2x + 1$ and $g(x) = 2x - 1$. Compare $(f+g)^{-1}(x)$ and $f^{-1}(x) + g^{-1}(x)$.

| | | | | |
|-------------|---|---|---|---|
| x | 0 | 1 | 2 | 3 |
| f(x) | 0 | 3 | 1 | 4 |
| g(x) | 1 | 0 | 4 | 3 |

25. **ANALYZE** If a relation is not a function, then its inverse is sometimes, always, or never a function. Justify your argument.

26. **PERSISTENCE** Give an example of a function that is its own inverse.

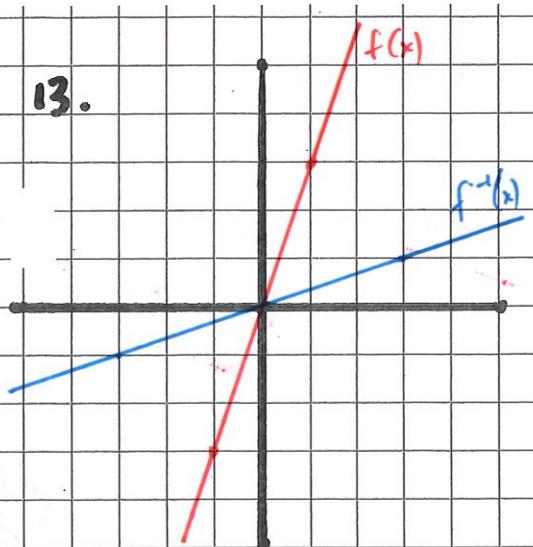
27. **WRITE** Suppose you have a composition of two functions that are inverses. When you put in a value of 5 for x , why is the result always 5?



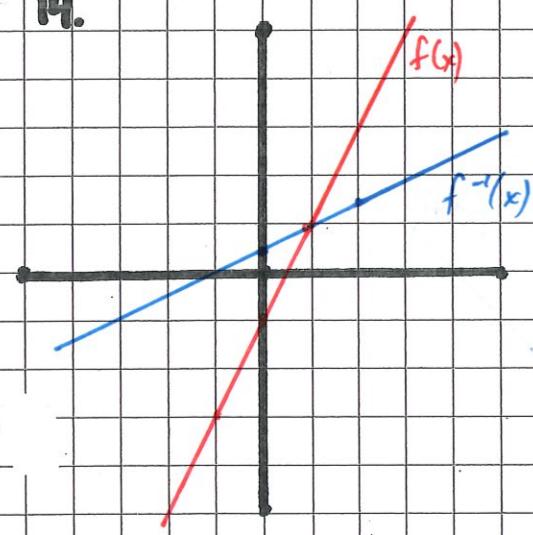
$f^{-1}(x)$

$f(x)$

13.



14.



15.

